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TRNSYS Type

Compressor heat pump including frost and cycle losses

Version 1.1

Model description and implementing into TRNSYS

Produced on behalf of the Swiss Federal Institute of Energy:

Low temperature low cost heat pump heating system

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Type401: Compression heat pump

General description

The heat pump is modeled as a black-box. The model is largely identical to that used in the YUM simulation program [1, 2]. The boundary conditions are the evaporator and condenser inlet temperature, the evaporator and condenser mass flow and the control signal of an external simulated controller.

The power of the condenser and the evaporator is calculated based on characteristic power curves which are usually supplied by the manufacturer of the heat pump. The curves show the condenser power and the electric power as a function of the evaporator inlet temperature and the condenser outlet temperatur (see Fig. 1). These values are used to calculate coefficients of biquadratic polynomials. The calculation of these coefficients has to be carried out with either the YUM simulation program or the program ‘polynom’ which is an extracted part of YUM. To increase the power of the heat pump by keeping the coefficient of performance (COP) constant, the condenser and the compressor power can be linearly scaled with a constant factor.

These polynomials are valid only for the steady state. To take the cycle losses of the heat pump into account, the computed power is corrected with the solution of a first order differential equation, known in the control theory as a PT_1-element.

The power reduction due to icing and defrosting can be computed with a semi-empiric approach in case it is not already included in the manufacturer documents. However, with this model, it is not possible to determine at which timestep the ice will be melted.

Based on validation of the YUM algorithm with measurement data the expected accuracy of the model is:

	Relative error
Condenser energy	6.6%
Compressor energy	12.5%
COP	2.7%

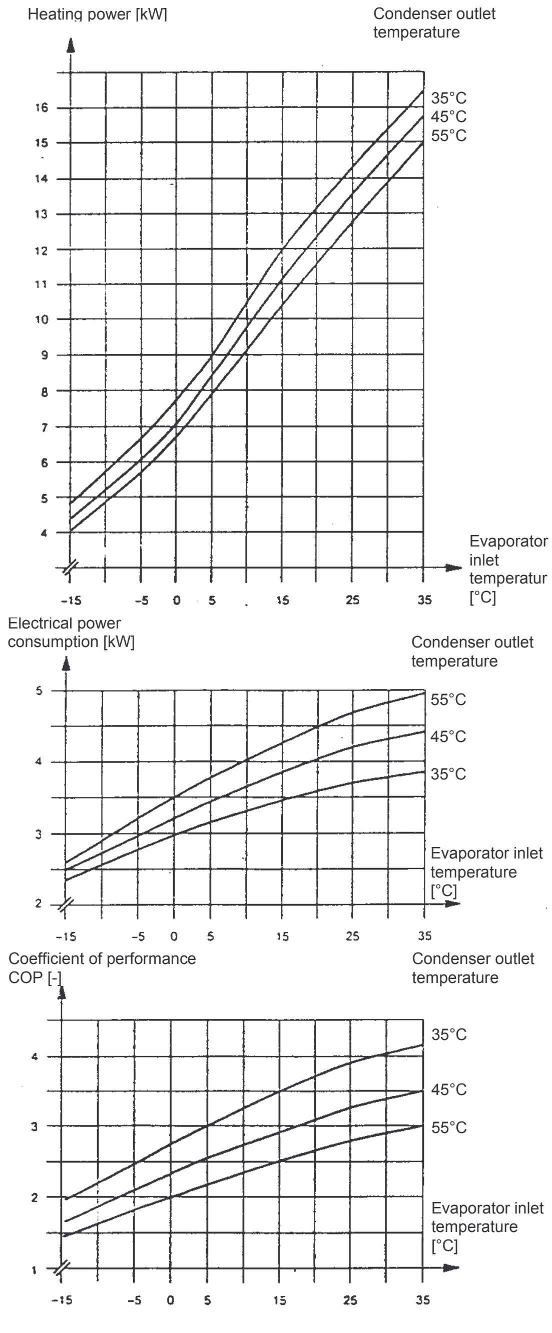

Fig. 1: Power characteristics of a heat pump.

Symbols

Variables

τ	Time constant
Δ	Difference
A	Constant for frost/defrost loss
B	Constant for frost/defrost loss
bp	Polynomial coefficient for compressor power
bq	Polynomial coefficient for condenser power
C	Constant for frost/defrost loss
c	Specific heat capacity
COP	Coefficient of performance
D	Constant for frost/defrost loss
E	Constant for frost/defrost loss
f	Scaling factor for heat pump power
m	Mass flow
P	Electrical power
Q	Heating power
T	Temperature
t	time

Indices

c	Condenser
corr	Corrected
e	Evaporator
f	Fictive
hp	Heat pump
ice	Icing/defrosting
icycle	Including cycle losses
in	Inlet
lb	Lower boundary
m	Mean value
n	Normalized
nom	Nominal value
off	Off
on	On
out	Outlet
plug	Power at the electrical terminals
ss	Steady state
ub	Upper boundary
wol	Without losses

Mathematical description

Sign convention: added power or energy is always positive, emitted always negative.

Steady state condenser and compressor power

After reading in the biquadratic polynomial coefficients which have to be determined with the external program 'polynom' or with YUM they are multiplied with a scaling factor:

$$bq_i := f\ bq_i \quad for\ i = 1...6$$
$$bp_i := f\ bp_i \quad for\ i = 1...6$$

Eq. 1

The steady-state power is then computed with the biquadratic polynomial:

$$Q_{ss,c,wol} = bq_1 + bq_2\ T_{n,e,in} + bq_3\ T_{n,c,out} + bq_4\ T_{n,e,in}\ T_{n,c,out} + bq_5\ T_{n,e,in}^2 + bq_6\ T_{n,c,out}^2$$

Eq. 2

$$P_{ss,plug} = bp_1 + bp_2\ T_{n,e,in} + bp_3\ T_{n,c,out} + bp_4\ T_{n,e,in}\ T_{n,c,out} + bp_5\ T_{n,e,in}^2 + bp_6\ T_{n,c,out}^2$$

Eq. 3

In the polynomial, normalized temperatures according to the formula

$$T_n = \frac{T\,[^\circ C]}{273.15} + 1.0$$

Eq. 4

are used.

Iteration of condenser outlet temperature

The condenser outlet temperature is used as an independent variable in Eq. 2 and Eq. 3. Since the condenser outlet temperature is also dependent of the result of Eq. 2 and Eq. 3, it must be calculated iteratively. The iteration is carried out with the Van Wijngaarden-Decker-Brent algorithm [3]. This algorithm combines the stability of the bisection with the calculation speed of the inverse quadratic interpolation.

Cycling losses

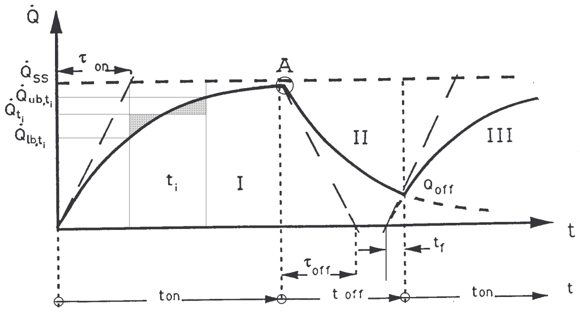

Fig. 2: Cycling losses shown with an example of a discrete timestep.

After the heat pump is switched on, the machine has to be heated up and the pressure difference between the evaporator and the condenser must be built up. This leads to a power reduction during the heat-up process. The power reduction during the heat-up process of a completely cooled down heat pump (area I) can be written with

$$\Delta\dot{Q}_{on,c} = \dot{Q}_{ss,c}\; e^{-\frac{t_{on}}{\tau_{on}}}$$

Eq. 5

In the case that the heat pump has not cooled down completely, the switch-on time can be transformed according to Fig. 2 (area III). Eq. 5 can therefore be written as:

$$\Delta\dot{Q}_{on,c} = \dot{Q}_{ss,c}\; e^{-\frac{t_f + t_{on}}{\tau_{on}}}$$

Eq. 6

The effective condenser power (without icing and defrosting losses) can then be caculated according to:

$$\boxed{\begin{aligned}\dot{Q}_c &= \dot{Q}_{ss,c} - \Delta\dot{Q}_{on,c}\\ &= \dot{Q}_{ss,c}\left(1 - e^{-\frac{t_f + t_{on}}{\tau_{on}}}\right)\end{aligned}}$$

Eq. 7

The time shift t_f is computed every time the heat pump is switched on. Because the running time t_{on} is equal to 0 when the heat pump is switched on (border of area II and area III), the time shift t_f can be calculated according to

$$\dot{Q}_{lb,c} = \dot{Q}_{ss,c}\left(1 - e^{-\frac{t_f}{\tau_{on}}}\right)$$

Eq. 8

Eq. 8 solved for the required time shift t_f is

$$t_f = -\tau_{on}\,\ln\left(1 - \frac{\dot{Q}_{lb,c}}{\dot{Q}_{ss,c}}\right)$$

Eq. 9

If the heat pump is not running, its energy is assumed to decrease exponentially. Therefore, the starting point of the cool-down function must be known (Fig. 2, point A). For calculating the starting point of the cool-down curve, the power at the upper boundary of the current time interval must be calculated at every time step during the operating phase using the expression

$$\dot{Q}_{ub,c} = \dot{Q}_{ss,c}\left(1 - e^{-\frac{t_f + t_{on,ub}}{\tau_{on}}}\right)$$

Eq. 10

The cool-down curve in Fig. 2 (area II) is calculated analogously to the heating reduction described previously:

$$\dot{Q}_{loss,c} = \dot{Q}_{ss,c,nom}\; e^{-\frac{t_f + t_{off}}{\tau_{off}}}$$

Eq. 11

The cool-down process is assumed to be proportional to the nominal power of the heat pump (at 7°C evaporator inlet temperature and 35°C condenser outlet temperature). Therefore, the time constant for the cool-down process which is derived from measurement data has to be based on this nominal power.

The time shift t_f is analogously to the approach of Eq. 8, but with a decreasing exponential function:

$$\dot{Q}_{lb,c} = \dot{Q}_{ss,c,nom} \; e^{-\frac{t_f}{\tau_{off}}}$$

Eq. 12

$$t_f = -\tau_{off} \; \ln\left(1 - \frac{\dot{Q}_{lb,c}}{\dot{Q}_{ss,c,nom}}\right)$$

Eq. 13

The power at the lower boundary of the interval of the current timestep t is equal to the power at the upper boundary of the last timestep t-Δt. The latter is already computed with Eq. 10.

Therefore, the cycle loss at the upper boundary of the current time interval is given by

$$\dot{Q}_{ub,c} = \dot{Q}_{ss,c,nom} \; e^{-\frac{t_f + t_{ub}}{\tau_{off}}}$$

Eq. 14

where t_{ub} is the difference between the upper boundary of the current time interval and the shut-down time.

This value will be used if the heat pump is switched on again in the next timestep.

The mean condenser power over the current timestep is calculated using the integral of the power (Eq. 7) over the timestep

$$\dot{Q}_{m,c} = \frac{1}{\Delta t} \int_{t_{lb}}^{t_{ub}} \dot{Q}_c \; dt$$

$$= \dot{Q}_{ss,c}\left(1 + \frac{\tau_{on}}{\Delta t} \; e^{-\frac{t_f}{\tau_{on}}} \left(e^{-\frac{t_{ub}}{\tau_{on}}} - e^{-\frac{t_{lb}}{\tau_{on}}}\right)\right)$$

Eq. 15

The COP is therefore, taking the cycling losses into account:

$$COP_{icycle} = \frac{-\dot{Q}_{m,c}}{P_{plug}}$$

Eq. 16

Icing and defrosting of the evaporator

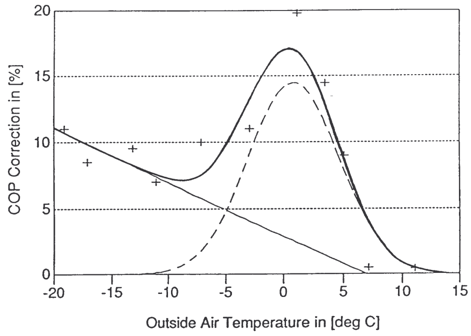

Fig. 3: COP reduction due to icing and defrosting of the evaporator. (Dots indicate measurement data)

The relative variation of the COP due to frosting and defrosting of the evaporator is described by a modified Gauss curve [4] (see Fig. 3).

The curve results from a superposition of a Gauss curve with a straight line. The Gauss approximation represents the maximal frost occurrence between 0°C and +5°C (high absolute air humidity). The straight line stands for the energy input for defrosting, which increases with decreasing outside air temperature. This energy is used for heating up the metal of the evaporator, the refrigeration in the evaporator and the heating up and melting of the ice.

The relative variation of the COP can therefore be calculated according to:

$$For\; A + BT_{e,in} > 0:$$

$$\Delta COP_{ice} = A + BT_{e,in} + Ce^{-\frac{(T_{e,in} - D)^2}{E}}$$

$$For\; A + BT_{e,in} \leq 0$$

$$\Delta COP_{ice} = Ce^{-\frac{(T_{e,in} - D)^2}{E}}$$

Eq. 17

The COP in consideration of all losses (cycle loss, icing and defrosting) can be computed with:

$$\boxed{COP_{corr} = COP_{icycle}\left(1 - \Delta COP_{ice}\right)}$$

Eq. 18

Condenser and evaporator power

With the corrected coefficient of performance COP_{corr}, the condenser and evaporator power can be calculated according to

$$\dot{Q}_{m,c} = -\,COP_{corr}\ P_{plug}$$

Eq. 19

$$For\ \ -\left(\dot{Q}_{m,c} + P_{comp}\right) > 0$$
$$\dot{Q}_{m,e} = -\left(\dot{Q}_{m,c} + P_{comp}\right)$$
$$For\ \ -\left(\dot{Q}_{m,c} + P_{comp}\right) \le 0\ .$$
$$\dot{Q}_{m,e} = 0$$

Eq. 20

Finally, the outlet temperature of the condenser and evaporator can be computed with:

$$T_{c,out,corr} = T_{c,in} - \frac{\dot{Q}_{m,c}}{\dot{m}_c c_c}$$

Eq. 21

$$T_{e,out,corr} = T_{e,in} - \frac{\dot{Q}_{m,e}}{\dot{m}_e\ c_e}$$

Eq. 22

Heat pump mode

The variable hpmode is set on the output #12. Its an indicator that shows in which mode the heat pump is currently operating. The following modes are possible:

hpmode	Description
100	Heat pump on, usual operation
200	Heat pump switched off due to signal from external controller (yhp=0)
210	Low-pressure error. Evaporator inlet temperature lower than low-pressure thermostat
220	Low-pressure error. Evaporator outlet temperature lower than low-pressure thermostat
230	Low-pressure error. No mass flow through evaporator
250	High-pressure error. Condenser inlet temperature higher than high-pressure thermostat
260	High-pressure error. Condenser outlet temperature higher than high-pressure thermostat
270	High-pressure error. No mass flow through condenser

Component configuration

Parameter	Fortran variable	Description
1	scale	Scale factor for heat pump power
2	ce	specific heat of evaporator fluid
3	cc	specific heat of condenser fluid
4	Pcar	power of carter heating
5	loprth	Set point of low-pressure thermostat (temperature)
6	hiprth	Set point of high-pressure thermostat (temperature)
7	airhp	Flag for evaporator icing/defrosting (0: No icing/defrosting is calucated, 1: Icing/defrosting is calculated)
8	COPcorr1	1st COP correction value on straight line of frost curve
9	COPcorr2	2nd COP correction value on straight line of frost curve
10	COPcorr3	Maximum COP correction on Gauss curve (*not* on the superposition of the Gauss curve and the straight line!)
11	Tdbcorr1	Outside air temperature at 1st COP correction value
12	Tdbcorr2	Outside air temperature at 2nd COP correction value
13	Tdbcorr3	Outside air temperature at maximum of Gauss curve
14	Tdbcorr4	Width (temperature) of the gauss curve on the half height of the Gauss maximum
15	tauon	Heat-up constant, related to the mean operation power
16	tauoff	Cool-down constant, related to evaporator inlet temp. +7°C and condenser outlet temp. +35°C
17	nchangemax	Maximal number of changes of the heat pump mode during a TRNSYS timestep
18	LUNbq	Logical unit number of file that contains the polynomial coefficient of the condenser power
19	LUNbp	Logical unit number of file that contains the polynomial coefficient of the compressor power

assign *filename LUNbq*

assign *filename LUNbp*

Both files have to be generated with either YUM or polynom. If the YUM-files are used, the first 10 rows have to be expanded to 80 character (fill in blanks).

Input	Fortran variable	Description
1	mdote	Mass flow evaporator
2	Tein	Inlet temperature evaporator
3	mdotc	Mass flow condenser
4	Tcin	Inlet temperature condenser
5	yhp	Control signal for heat pump (0: off, 1: on)
6	ycar	Control signal for carter heating (0: off, 1: on)

Output	Fortran variable	Description
1	mdote	Mass flow evaporator
2	Teout	Outlet temperature evaporator
3	mdotc	Mass flow condenser
4	Tcoutc	Outlet temperature condenser
5	Qdotmc	Mean condenser power over the timestep
6	Qdotme	Mean evaporator power over the timestep
7	Pcomp	Compressor power
8	Pcar	Carter heating power
9	(Pcomp+ Pcar)	Sum of compressor and carter heating power
10	COPc	Coefficient of performance, including cycling and icing/defrost losses
11	deltCOP	Relative COP reduction due to icing/defrost losses
12	hpmode	Operation mode of heat pump
13	switch	Number of heat pump switch-ons since start of simulation
14	timeint	If the heat pump is changed from not running to running in the *current* timestep: Timedifference between the last switch on signal and the current timestep, otherwise: timeint = 0.

Literature

1 Afjei Thomas; YUM, A Yearly Utilization Model for Calculating the Seasonal Performance Factor of Electric Driven Heat Pump Heating Systems, Technical Form; Eidgenössische Technische Hochschule Zürich, IET-LES; Zürich 1989; Schweiz

2 Afjei Thomas, Wittwer Dieter; Yearly Utilization Model YUM WP/Holz, Benutzerhandbuch mit Beispielen; INFEL/KRE; Zürich 1995; Schweiz

3 Press William H., Flannery Brian P., Teukolsky Saul A., Vetterling William T.; Numerical Recipes, The Art of Scientific Computing; ISBN 0 521 30811 9; Cambridge University Press; Cambridge MA 1987; USA

4 Conde M. R.; Progress Report IEA-Annex 10, Air-to-Water Heat Pump, Simple Simulation Model; Eidgenössische Technische Hochschule Zürich, IET-LES; Zürich 1985; Schweiz